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# VAR, VA, AND 4 QUADRANT METERING



Monday, July 10<sup>th</sup>, 2023

1:45 PM - 2:45 PM

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#### VAR, VA, and 4 Quadrant Metering Agenda

1	Power Review
2	VARs & VAs
3	Sources of Reactance
4	Metering W, VAR, VA
5	4 Quadrant Metering
6	Power Quality





#### **POWER THEORY REVIEW**

#### Ohm's Law and Power Calculations



**OHM'S LAW** 

- Ohm's Law provides basic formulas used for calculating power.
- The law states that the current, I, through a conductor is directly proportional to the voltage, E.
- The figure to the right provides all the power related formulas derived from Ohm's Law.



Ohm'sLaw



• In a basic DC circuit, we can use Ohm's Law to calculate the current for this circuit

• 
$$I = \frac{E}{R_1 + R_2}$$

- Then we can calculate the power consumed by the load  $P = I^2 \times R_2$
- R<sub>1</sub> reflects resistant in line from source to load, and R<sub>2</sub> is the resistance of the load. In most cases R<sub>2</sub> would be much greater than R<sub>1</sub>. Thus, most of the power is consumed by the load.
- These are the same basic applied to metering to measure the power and energy consumed by the load.





#### DC vs. AC Circuits

- Capacitors are resistive elements in a circuit that don't have real resistance, but reactance
- In AC circuits they create an induced current that affects the phase relationship between voltage and current for that phase
- A cap bank is an example of a capacitor
- Capacitive Reactance is defined as; X

$$_{C}=\frac{1}{2\pi fC}$$

- Inductors similarly are resistive elements in a circuit that don't have real resistance, but reactance
- Like capacitors, in an AC circuit they induce a current into the circuit that affects the phase relationship between voltage and current for that phase
- A transformer is an example of an inductor. Most loads have inductive elements/models
- Inductive Reactance is defined as;  $X_L = 2\pi f L$

Inductance

Capacitance





- Capacitors and inductors behave differently in AC circuits compared to DC circuits
- In DC circuits a Capacitor will look like an open circuit after fully charging; RC time constant







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- In DC circuits a Capacitor will look like an open circuit after fully charging; RC time constant
- Inductors will look like a short circuit after fully charging; 1/RL time constant







- Capacitors and inductors behave differently in AC circuits compared to DC circuits
- In DC circuits a Capacitor will look like an open circuit after fully charging; RC time constant
- Inductors will look like a short circuit after fully charging; 1/RL time constant
- In AC circuits inductors and capacitors induce a current that causes a phase displacement with the source current. R is replaced with impedance Z; Z = R + jX





How does inductance and capacitance affect AC power?

In inductive (L) circuits, voltage
(E) leads current (I) - ELI



In a capacitive (C) circuit, current
(I) leads voltage (V) - ICE



Inductor – Voltage leads Current

Capacitor – Current leads voltage



### **AC POWER CALCULATIONS**



Single Phase Apparent Power(VAs) =  $V_{A_{rms}} \times I_{A_{rms}}$ 

- When calculating AC power you must account for the phase angle difference between the voltage and current signals.
- You will notice there are 3 calculations for AC single phase power. We will cover the differences in more detail later
- The signals to the left are at unity PF
- The base formula of AC power is still;

P = I X E

AC Power Calculations



#### **CALCULATING ENERGY**



Calculating Energy

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- A, B, and C are constant in the equation
- Energy can be simplified at calculating the area under the curve
- High sampling rates provide small distances between data points and reduce error introduce from noise by keeping the line between points flat
- Energy is the sum of the area of each section using the trapezoid formula for area

### SINGLE PHASE POWER & ENERGY





- Energy accumulation on a sample-by-sample analysis
- Energy accumulation accelerates at peaks and decreases at negative peaks
- When power wave crosses X axis energy will fall, or have a negative slope
- Higher sampling rates provided a more rounded curve, and increase accuracy





- In a balanced 3 phase load, the power total is constant on a sample by sample analysis!
- Energy accumulates in a linear progression
- This is only true when power is balanced
- When power is unbalanced the energy accumulation isn't linear



The Power Triangle





- VA stands for Volt-Amps
  - VA represents the total demand of a load
  - It doesn't account for phase relationship in calculation, and is determined by the magnitude of voltage and current

Single Phase Apparent Power(VAs) =  $V_{A_{rms}} \times I_{A_{rms}}$ 

- VAR stands for Volt-Amps Reactive
  - VARs represents the power lost to reactive components, usually as heat.
  - VARs are a result of reactive loads like inductors and capacitors
  - Calculation for VARs is very similar to calculation for power but uses the sin function instead of cosine.

Single Phase Reactive Power (VARs) =  $V_{A_{rms}} \times I_{A_{rms}} \times \sin(\phi_{V_A} + \phi_{I_A})$ 



• Active power (P) is defined by the following calculation;

Single Phase Real Power (Watts) =  $V_{A_{rms}} \times I_{A_{rms}} \times \cos(\phi_{V_A} + \phi_{I_A})$ 

• Reactive power (Q) is defined by the following calculation;

Single Phase Reactive Power (VARs) =  $V_{A_{rms}} \times I_{A_{rms}} \times \sin(\phi_{V_A} + \phi_{I_A})$ 

• Apparent power (S) is defined by the following calculation;

Single Phase Apparent Power(VAs) =  $V_{A_{rms}} \times I_{A_{rms}}$ 

• And the relationship between all three of these quantities is;

$$S=\sqrt{R^2+Q^2}$$



- Trigonomic functions like sine/cosine have a triangular relationship that relates to power
- In the AC power calculations, you'll notice that real power calculation include the cosine function
- VARs use the sine function.
- When you calculate out the unity circle the cos(x) value also correlates to PF
- Cos(0) = 1, and sin(0) = 0, Unity PF



- We'll also look at some common reference points, and their PF values
- 30 degrees-
  - cos(30) = 0.866
  - sin(30) = 0.5
  - PF = 86.7%



- We'll also look at some common reference points, and their PF values
- 45 degrees-
- cos(45) = 0.707
- sin(45) = 0.707
- PF = 70.7%





- We'll also look at some common reference points, and their PF values
- 60 degrees-
- cos(60) = 0.5
- sin(60) = 0.866
- PF = 50%





- We'll also look at some common reference points, and their PF values
- 90 degrees-
- cos(90) = 0
- sin(90) = 1
- PF = 0%





- We can populate the rest if the unity circle the same values for every multiple of 30, 45, 60, and 90 degrees
- This can be used to quickly identify watt/var relationships and PF at specific points
- We calculate the X and Y axis using cosine and sine functions. Similar to calculate watts and vars
- Apparent power is also represented in the unity circle by the radius





- The unity circle ties directly into the power triangle and 4 quadrant metering
- We're going to calculate power at 15 degrees.





- The unity circle ties directly into the power triangle and 4 quadrant metering
- We're going to calculate power at 15 degrees.
  - Cos(15) = 0.966
  - Sin(15) = 0.259
  - PF = 96.6%





- The unity circle ties directly into the power triangle and 4 quadrant metering
- Next, we'll assume 120  $V_{\text{rms}}$  and 5  $A_{\text{rms}}$ 
  - This comes to 600 VA
  - 600 VA \* 0.966 = 579.6 W
  - 600 VA \* 0.259 = 155.4 VAR





• Next we'll use the AC power calculations;

• Understanding the unity circle and the mathematical relationship between P, S, and Q will help understanding 4 quadrant metering



#### **POWER FACTOR CALCULATIONS**



$$PF = \frac{Active \ Power \ (W)}{Apparent \ Power \ (VA)}$$

- Calculation to PF is straight forward, but there are 2 common sign conventions for PF
- IEC: Positive Active Power is Positive PF
- IEEE: Leading PF is positive, and Lagging is negative

Power Factor Calculations







#### Sources of Reactance







- Most AC loads have some amount of inductance
- Transformers are essentially large inductors and major sources of inductive reactance
- Cap banks are large capacitors used to offset inductive reactance on the system
- Base load power plants like coal, natural gas, and nuclear have good control on power factor output
- Transmission lines also have impedance that is directly proportional to the length of the line
- Power lines also have some capacitance between earth ground. A capacitor is essentially 2 electrical plates with a dielectric between them, like air.



#### **Power Lines**



- Any powerline of enough length will generate losses
- Longer lines will have greater losses, and see voltage drop
- Can calculate impedance from cross sectional area of cable, number of cable, and length





- Power transformers used to step and step down voltage have core and wiring losses associated with them
- A power transformer is basically a large inductor and most of the losses are lost as heat and represented as VARs
- Transformer losses can be found on the manufacturers test report





- Capacitor banks are used for VAR correction and voltage optimization
- They're basically large caps, and are rated in VARs at system frequency
- They do consume a small amount of active power as well





#### **CUSTOMER LOADS**



- Customer loads will vary from residential to commercial and industrial loads
- PF may vary from 85% up to 95%+
- Most agreements with large customers have minimum PF requirements
- Customers are only billed on Watts, so poor PF is essentially lost revenue

IDENTIFYING POWER FROM VOLTAGE AND CURRENT SIGNALS



• What can you tell me about these signals and their power measurements-

P = S Q = 0 PF = 100% or Unity Delivered Watts

Identifying Power from Voltage and Current Signals




- What can you tell me about these signals and their power measurements-
  - Voltage leads Current Inductive Load P=Q Active Power Delivered Reactive Power Delivered

Identifying Power from Voltage and Current Signals





• What can you tell me about these signals and their power measurements-

Voltage lags Current Capacitive Load P=Q Active Power Delivered Reactive Power Received

Identifying Power from Voltage and Current Signals





 What can you tell me about these signals and their power measurements-

> Current and voltage are 180 degrees apart P = S Q = 0 PF = -100% or Unity Received Watts, -P

Identifying Power from Voltage and Current Signals

# HOW TO MEASURE PHASE SHIFT





- Distance from Peak to Peak = 1 cycle
- Our electric grid is 60 Hz, or 60 cycles/sec
- 1 cycle/period = 16.6 ms
- V1 peak to l1 peak is phase difference between signals; 1.389 ms
- Voltage leads current tells us this is an inductive circuit
- The phase angle difference between the two signals is-

PS = 360 \* td/p

## HOW TO MEASURE PHASE SHIFT





PS = 360 \* td/p

- PS is the phase shift in degrees
- td is time difference
- p is period or length of 1 cycle
- td and p need to use the same measurement, like seconds or milli-seconds

= 30 degrees

How to measure Phase Shift

### SYSTEM OVERVIEW



#### **Circuit Analysis Point of View**





### SYSTEM OVERVIEW

Could look something like this





### SYSTEM OVERVIEW



This example doesn't reflect an actual study MVA demand from all the loads is 140 MVA Only 103 MW is billed VARs are a result of reactive loads on the system that are dispersed as heat

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### METERING W, VAR, VA





Schneider Electric Life Is On

A Polar

0000:



- So far, we've primarily looked at AC power by looking at waveshapes and sampled values
- Power meters analyze these values, and calculate the RMS values for each input
  - In previous formulas I've used RMS values in the power formulas
- Meters can provide high speed RMS values; updates several times a second down to half-cycle RMS values
- Many meters update once a second and provide RMS and fundamental values;
  - RMS values include distortion; sampling rate affects how much distortion is captured
  - Fundamental values only account for the 60 Hz signal



Root Mean Square of Data Points





- RMS refers to the root of the average of the squares for a set a data
- For our purposes these are the sampled values.
- To the right is an example set for a signal that samples at 8 samples/cycle

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- First Step is to square all the sampled values

Root M	ean Square	of Data	Points
--------	------------	---------	--------

V1	V1	S	quare
16	9.7116	9.72	8800.00
120	0.0102	0.00	4400.00
(	0.00	0.00	0.00
-12	0.0102	0.00	4400.00
-16	9.7116	9.72	8800.00
-12	0.0102	0.00	4400.00
(	0.00	0.00	0.00
12	0.0102	0.00	4400.00





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Root Mean Square of Data Points

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- To the right is an example set for a signal that samples at 8 samples/cycle
- First Step is to square all the sampled values
- Then, calculate the average of the squares

V1 V1	So	uar <b>e</b> qu	are M	ean
169.71	69. <b>72</b> 8	8002 <b>88</b>	00.00	400.00
120.00	20.0104	4001 <b>00</b>	00.00	
0.00	0.00	0.00	0.00	
-120.00	20.0104	4001 <b>00</b>	00.00	
-169.71	69. <b>72</b> 8	8002 <b>88</b>	00.00	
-120.00	20.0104	4001 <b>00</b>	00.00	
0.00	0.00	0.00	0.00	
120.00	20.0104	4001 <b>00</b>	00.00	

- RMS refers to the root of the average of the squares for a set a data
- For our purposes these are the sampled values.
- To the right is an example set for a signal that samples at 8 samples/cycle
- First Step is to square all the sampled values
- Then, calculate the average of the squares
- Finally, calculate the square root of the average, of the squares

Root Mean Squar	e of Data Points
-----------------	------------------

	-						
V	1 V	1 Squ	lareSqu	are Me	ean Me	an Ro	ot
	169.71	69. <b>28</b>	800. <b>28</b>	800.04	100. <b>00</b> 4	00.00	120
	20.00	20.004	100. <b>0<del>0</del></b>	00.00			
	0.00	0.00	0.00	0.00			
-'	120.00	20.04	100. <b>0<del>0</del></b>	00.00			
-'	169.71	69. <b>28</b>	300. <b>28</b>	800.00			
-'	120.00	20.04	100. <b>00</b>	00.00			
	0.00	0.00	0.00	0.00			
	20.00	20.04	400. <b>00</b>	00.00			





## **RMS VALUES**

#### Root Mean Square of Data Points

- RMS refers to the root of the average of the squares for a set a data
- For our purposes these are the sampled values.
- To the right is an example set for a signal that samples at 8 samples/cycle
- First Step is to square all the sampled values
- Then, calculate the average of the squares
- Finally, calculate the square root of the average, of the squares
- More simply, the RMS value can be calculated by taking the peak and dividing by the square root of 2.
- RMS is also the equivalent DC voltage level



$$V_{RMS} = \frac{V_{PEAK}}{\sqrt{2}} = \frac{169.71}{\sqrt{2}} = 120 V$$



Root Mean Square of Data Points

• Calculations for 3 element connected meters

3 Phase Active Power (Watts) =  $V_{A_{rms}} \times I_{A_{rms}} \times \cos(\phi_{V_A} + \phi_{I_A}) + V_{B_{rms}} \times I_{B_{rms}} \times \cos(\phi_{V_B} + \phi_{I_B}) + V_{C_{rms}} \times I_{C_{rms}} \times \cos(\phi_{V_C} + \phi_{I_C})$ 3 Phase Active Power (VARs) =  $V_{A_{rms}} \times I_{A_{rms}} \times \sin(\phi_{V_A} + \phi_{I_A}) + V_{B_{rms}} \times I_{B_{rms}} \times \sin(\phi_{V_B} + \phi_{I_B}) + V_{C_{rms}} \times I_{C_{rms}} \times \sin(\phi_{V_C} + \phi_{I_C})$ 3 Phase Active Power (VAs) =  $V_{A_{rms}} \times I_{A_{rms}} + V_{B_{rms}} \times I_{B_{rms}} + V_{C_{rms}} \times I_{C_{rms}}$ 

• Calculations for 2 element connected meters

3 Phase Active Power (Watts) =  $V_{AB_{rms}} \times I_{A_{rms}} \times \cos(\phi_{V_{AB}} + \phi_{I_A}) + V_{BC_{rms}} \times I_{B_{rms}} \times \cos(\phi_{V_{BC}} + \phi_{I_B})$ 3 Phase Active Power (VARs) =  $V_{AB_{rms}} \times I_{AB_{rms}} \times \sin(\phi_{V_{AB}} + \phi_{I_A}) + V_{BC_{rms}} \times I_{B_{rms}} \times \sin(\phi_{V_{BC}} + \phi_{I_B})$ 3 Phase Active Power (VAs) =  $V_{AB_{rms}} \times I_{A_{rms}} + V_{BC_{rms}} \times I_{B_{rms}}$ 



### **COMPLEX CALCULATIONS**

→ V2

→ V3

**>**11



 $\boldsymbol{C} = \boldsymbol{A} * \sin(2\pi \boldsymbol{f} \boldsymbol{t} + \boldsymbol{\theta})$ 

- The waveshape form is:
  - A indicates the peak magnitude of the signal
  - 2 $\Omega f$  is the angular frequency
  - t represents time, usually reference to 0
  - θ indicates displacement to reference signal in radians



Phasor Diagram

- The polar form is:
  - Z indicates magnitude only
  - The phase angle (θ) is measured counterclockwise from the positive real axis



### C = X + jY

- The rectangular form is:
  - X indicates the real axis
  - jY indicates the imaginary axis



- The previous 3 calculations are all used to calculate correlated values for voltage and current signals
- Samples values are used to calculate RMS and phase angle values used in polar coordinates
- Polar coordinate and rectangular coordinates represent the same values, but in different forms
  - Polar coordinates are ideal for comparing the phasor relationship between voltage and current elements
  - Rectangular coordinates are helpful for applying complex math to phasor values
- Complex Math
  - You can multiply and divide polar coordinate, but cannon add and subtract
  - You can add and subtract rectangular values for Net calculations



## **ENERGY METER QUANTITIES**

- Meters today provide real time outputs for;
  - Active Power & Energy
  - Reactive Power & Energy
  - Volt-Amp Power & Energy
  - Per phase values for volts, amps, and power
  - 4 quadrant, bi-directional metering
  - And more...!
- Data can be collected real time utilizing SCADA, or through data recorders connected to a billing system like MV90







- Power can be broken into 4 quadrants based on direction of active power and reactive power
  - +P and +Q is upper right Quadrant 1
  - -P and +Q is upper left Quadrant 2
  - -P and -Q is lower left Quadrant 3
  - +P and -Q is lower right Quadrant 4





#### Quadrant or Quantity



• Active energy delivered is Q1+Q4



#### Quadrant or Quantity



- Active energy delivered is Q1+Q4
- Active energy received is Q2+Q3



#### Quadrant or Quantity



- Active energy delivered is Q1+Q4
- Active energy received is Q2+Q3
- Reactive energy delivered is Q1+Q2



#### Quadrant or Quantity



- Active energy delivered is Q1+Q4
- Active energy received is Q2+Q3
- Reactive energy delivered is Q1+Q2
- Reactive energy received is Q3+Q4



- Most customer loads will fall into Quadrant 1, from utility perspective
  - Active power is delivered to customer
  - Most customers will have an inductive impedance which will have reactive power delivered
  - Customers with PF correction may have near unity or reactive power received
- Bi-directional meters will primarily fall into Q1 and Q3
  - Active power delivered and reactive power delivered
  - Active power received and reactive power received
- Loads in Q2 and Q4 has greater capacitive reactance than inductive, most likely due to PF correction devices
- Some generators can output power in Q4 to compensate for low system PF



- Configuration 1 captures all active and reactive energy
- Configuration 2 captures all active energy, and only reactive energy in inductive quadrants
- Configuration 3 captures all active and reactive energy, but splits out reactive energy into quadrants
- Preference depends on what power factor correction a customer uses and how to capture it

Channel 1: kWh del Channel 2: kWh rec Channel 3: kVARh del Channel 4: kVARh rec Channel 1: kWh del Channel 2: kWh rec Channel 3: kVARh Q1 Channel 4: kVARh Q3 Channel 1: kWh del Channel 2: kWh rec Channel 3: kVARh Q1 Channel 4: kVARh Q2 Channel 5: kVARh Q3 Channel 6: kVARh Q4

Configuration 1





- We'll focus on Power Factor and Voltage Loss
  - Poor PF can increase demand on the system that can't be recovered
  - Lines with significant impedance will see voltage loss over long distances
- Corrective devices
  - Cap Banks
  - Voltage Regulators and Transformer Tap Settings
  - Generator and inverter reactive power setpoints
  - Static Var Compensators
- VVO Software



**PF EXAMPLE** 



Let's assume \$0.10 kWh.

Usage bill at 85% PF would be ~\$7.2k

If PF could be increased to 90% PF for month usage bill ~\$7.6k

That's roughly \$400 a month or \$5k a year

For MW customers the cost will scale by that much!

If you have 100 similar customers that could be \$500k a year



### **VOLTAGE LOSS EXAMPLE**



VA Demand at Generator would be 1800 VA (secondary)

Accounting for power losses ( $I^2 * Z$ ) across system using supplied impedance. VA at customer is 1671.

Current remaining constant, calculate V to be-

VA 111 V VB 111 V VC 111 V



### **VVO DEVICES**





## **CAPACITOR BANKS**

- Capacitor banks are used for VAR correction and voltage optimization
- They're basically large caps, and are rated in VARs at system frequency
- They do consume a small amount of active power as well





- A power distribution voltage regulator is an auto transformer that can step-up or step-down voltage to provide consistent system voltage levels. A voltage regulator control senses system voltage and commands the tap changer to operate when voltage changes are needed.
- This can be done with power transformers with multiple tap settings to accomplish the same goal





### **GENERATOR CONTROL**



- Generators are capable of operating at leading power factors, but will reduce kVA output
- Reactive capability curve provides kVA and kVAR capability at different setpoints
- Synchronous generators can be setup as a synchronous condenser to pull VARs off the system





- A static VAR compensator (SVC) is a set of electrical devices for providing fast-acting reactive power on high-voltage electricity transmission networks
- The SVC is an automated impedance matching device, designed to bring the system closer to unity power factor. SVCs are used in two main situations:
- Connected to the power system, to regulate the transmission voltage ("transmission SVC")
- Connected near large industrial loads, to improve power quality ("industrial SVC")


- Volt/VAR Optimization (VVO) optimally manages system-wide voltage levels and reactive power flow to achieve efficient distribution grid operation.
- VVO assists distribution operators reduce system losses, peak demand or energy consumption using Conservation Voltage Reduction (CVR) techniques.





## Life Is On Schneider